







sensitive to initial conditions; this is one of the main properties of a confused system [11].

Secret Sharing Scheme based Shamir  $(t, n)$  threshold scheme to fulfill spread storage, was firstly created by Shamir in 1979. In  $(t, n)$  threshold scheme provided rule of sharing secret message among  $n$  shadow,  $t$  and  $n$  are positive integer numbers and  $t$  less or equal to  $n$ . The secret message can be recovered only with the number of shadows equal to  $t$  or more than  $t$ . The shadow array obtains from equation (4) [6]:

$$s(x_n) = m + s_1 x_n + \dots + s_{t-1} x_n^{t-1} \pmod{p} \quad (4)$$

## 2. Related Works

The related works can be classified into three domains: image cryptography based chaotic rule, secret sharing scheme, hiding the secret image in cover based on the chaotic rule.

In [10] presented a good steganography algorithm with two-stage authentication for secret image sharing, this algorithm provided an enhancement in both quality of stego image and security of secret image.

In [12] presented a new scheme for image steganography based on different size image segmentation (DSIS) and gives its modification.

In [13] presented an algorithm for image steganography with higher confidentiality and high capacity

based on Lorenz chaotic map and Kekre's Advanced Multiple LSB Algorithm (KAMLA).

In [1] developed a new technique for image steganography based on encrypted secret image by Lorenz, hide encrypted data with 3 level Discrete Wavelet Transform.

In [15] presented an algorithm for data encryption scheme based on cellular automata and chaotic map that employs piecewise linear nonlinearity, this scheme offers high level of security and fast processing time.

In [2] the proposed method gives a good distribution for the secret image among participant, this method based on  $(t, n)$  threshold secret sharing scheme, without loss of information.

In [7] the proposed an algorithm for image encryption with two-dimensional transform with a key quantum chaotic map, this rule, offers a high level security for information.

In [3] gave a new approach to secret image sharing with steganography, this approach can save storage space with enhances the quality of the secret image.

In [16] gave a new approach to secret image sharing based on linear cellular automata, hash functions, and digital signature to proposed a

novel (t,n) threshold image sharing scheme with steganography.

### 3. Proposed Method

The proposed algorithm in this paper contains two main parts: embedding part and extraction part.

In the embedding part, they are three phases: image encryption, secret sharing scheme and image steganography. The phases of the proposed algorithm are as follows, which is shown in **Fig. 1**.

**Phase1:** encrypts the secret image with Lorenz chaotic equations to increase the confidentiality.

**Phase2:** divides the encrypted image from phase1 to four shadows based on secret sharing scheme to distributed these shadows to the four cover images.

**Phase3:** embeds the shadows from phase2 with cover images based on random sequence generated from Lorenz equations.

#### A. Lorenz Encryption Phase

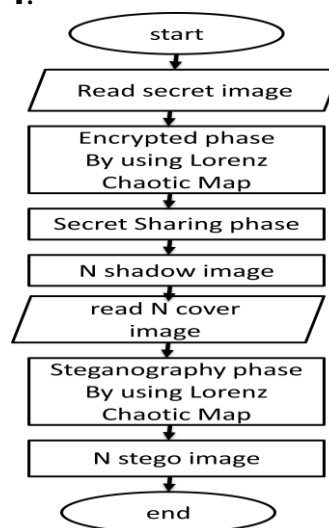
Random values with very sensitive to initial values are generated with Lorenz system. The encryption process for the secret image is done in the following steps which are shown in **Fig. 2**.

**Input:** secret image, secret key (32 ASCII char.), and sensitive parameters.

**output:** cipher image.

**steps:**

- 1) XOR function applied between fraction part from the mean of secret key and plain images as shown in **Fig. 3**. The result was enter to the Lorenz chaotic system.
- 2) Three array x, y, z are generated.
- 3) Apply some process on x,y,z arrays value are generated from step1 and change the value of the x,y in ascending sequence.
- 4) Save the index of the x arrays to generate key1.
- 5) XOR function applied between y and z array to generate key2.
- 6) Divided the secret image to blocks with size 8\*8.
- 7) Scrambling the bits for each block with key1.
- 8) XOR function applied on secret image with key2 array in the forms of row, column, lower triangular and upper with two directions triangular as shown in **Fig. 4**.



**Fig. 1** The proposed algorithm for embedding part.



### B. Secret Sharing Scheme Phase

Apply a (t, n) threshold scheme on the encrypted image to generate n different shadows. In the proposed algorithm, take t=4 and n=4. The process for sharing is done in the following steps which are shown in Fig. 5.

**Input:** cipher image.

**output:** n shadow.

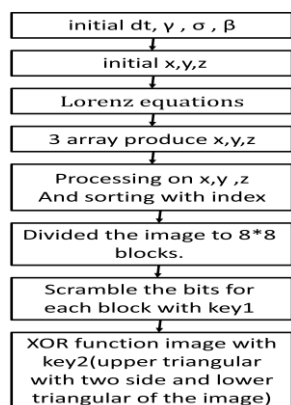
**steps:**

- 1) Reshape the input image to new dimension r rows and t columns.
- 2) For each row of the array from step 1, apply the Shamir's threshold scheme equation [6]:

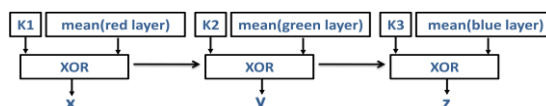
$$s_j(x_i) = s_{j0} + s_{j1}x_i + s_{j2}x_i^2 \pmod{257} \quad (5)$$

the value of base number equals 257. since the value of the color or gray image is between 0 and 255, 257 is the closest prime number to 255.

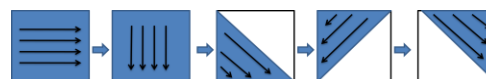
- 3) Repeat step 2 with n different integers values of  $x_1, x_2, x_3, x_4$ .
- 4) Four shadows  $s(x_1), s(x_2), s(x_3),$  and  $s(x_4)$  are generated.



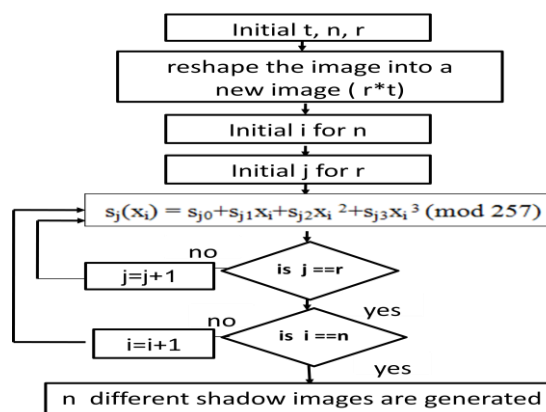
**Fig. 2 The encryption phase with Lorenz map.**



**Fig. 3 Generation the initial values for Lorenz map.**



**Fig. 4 The direction of the XOR function.**



**Fig. 5 The secret sharing phase.**

### C. Steganography Phase

Embedding process in this phase takes a randomly sequence based Lorenz equations, this process is done in the following steps which are shown in Fig. 6.

**Input:** n cover image, n shadow.  
**output:** n stego image.

**steps:**

- 1) x, y, z arrays are generated with new initial value.
- 2) For each i-th cover image divided into 8\*8 blocks.
- 3) select the blocks sequence with x, y, z arrays, with x, y selected the





sequence of the blocks in  $i$ -th cover and  $z$  selected the sequence of the pixels in the blocks.

- 4) Embedding the  $i$ -th shadow in blocks of  $i$ -th cover with pre-selected these blocks in step 3 with LSB method.

In secret sharing scheme phase with step2, It is possible that the value of the pixel in shadow equal 256, These values take nine bits rather than eight bits. In the proposed algorithm, for every eight pixels embedding nine bits with LSB for pixels as shown in **Fig. 7**, These step provided the maintain for the quality of the secret image when extracting.

$b_{11}...b_{14}...b_{17}b_{18}$	$b_{21}...b_{24}...b_{27}b_{28}$	$b_{31}...b_{34}...b_{37}b_{38}$	$b_{41}...b_{44}...b_{47}b_{48}$
$b_{51}...b_{54}...b_{57}b_{58}$	$b_{61}...b_{64}...b_{67}b_{68}$	$b_{71}...b_{74}...b_{77}b_{78}$	$b_{81}...b_{84}...b_{87}b_{88}$

(a)

$b_{11}...b_{14}...s1s2$	$b_{21}...b_{24}...b_{27}s3$	$b_{31}...b_{34}...b_{37}s4$	$b_{41}...b_{44}...b_{47}s5$
$b_{51}...b_{54}...b_{57}s6$	$b_{61}...b_{64}...b_{67}s7$	$b_{71}...b_{74}...b_{77}s8$	$b_{81}...b_{84}...b_{87}s9$

(b)

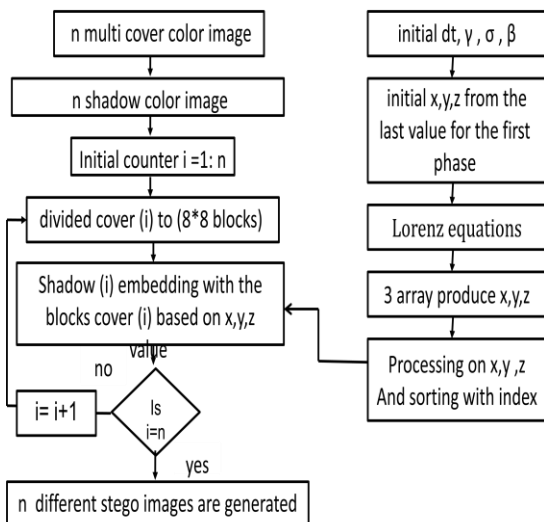
**Fig. 7 The embedding method, (a) 8-pixels of the 8\*8 pixels block in the cover image, (b) 9-Secret bits embedded with these pixels.**

In the extracting part, all the phases in embedding part applied with reverse direction, The phases of the proposed extracting algorithm are as follows, which is shown in **Fig. 8**.

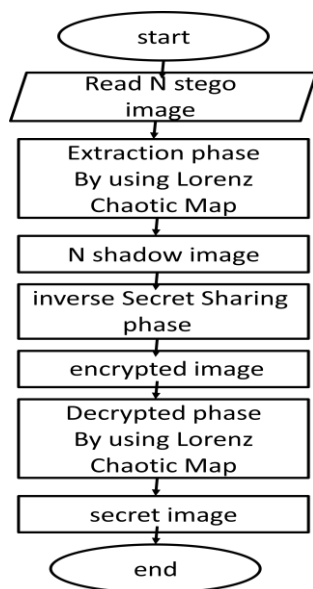
**Phase1:** extracted  $n$  shadows from  $n$  cover images based on the random sequence generated from Lorenz equations.

**Phase2:** inverse secret sharing scheme applied on  $n$  shadow to produce an encrypted secret image.

**Phase3:** Decrypts the secret image with Lorenz chaotic equations to produce the secret image.



**Fig. 6 Steganography phase.**



**Fig. 8** The proposed algorithm for extracting part.

## 4. Experimental Result

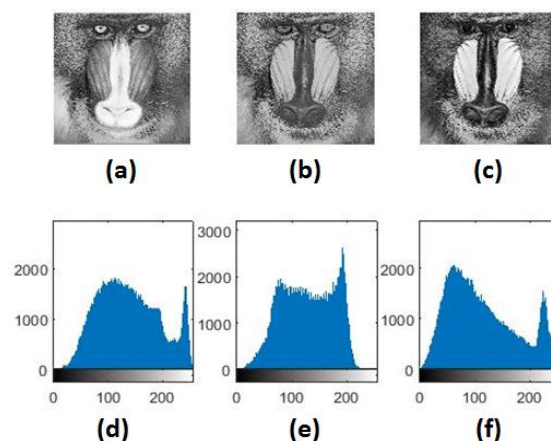
In proposed algorithm, two parts are performed in this section : In the first part, check the performance of proposed encryption algorithm with cipher image.

### A. Encryption and Histogram

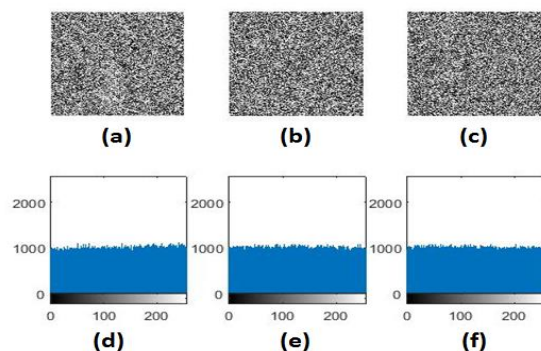
An ideal cipher image should have a uniform distribution about the frequency. Two images (baboon 512\*512 and sailboat 512\*512) from the USC-SIPI image database were used in the proposed encryption algorithm as shown in the **Fig. 9, 11**. These images tested with histogram, The result shown in the **Fig. 10, 12**. In the flowing the secret keys are used.

k1=Z&QBZH8ATBaCdaFEHijkk1-  
Z23456N#9

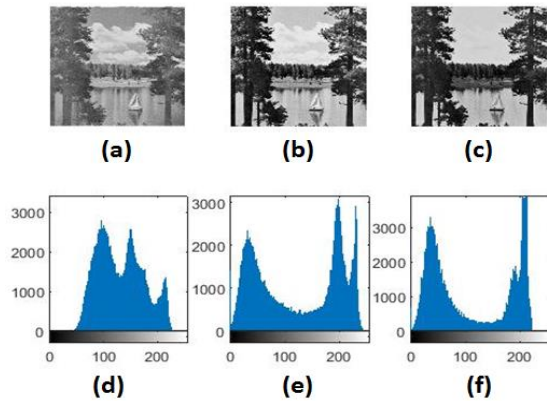
k2=B2BB5M7#AC%+cdEfgQijNkl  
m1M%4567#  
k3=BZHO56BZ8AAbCdeRgHiJk\*1  
%1234567#



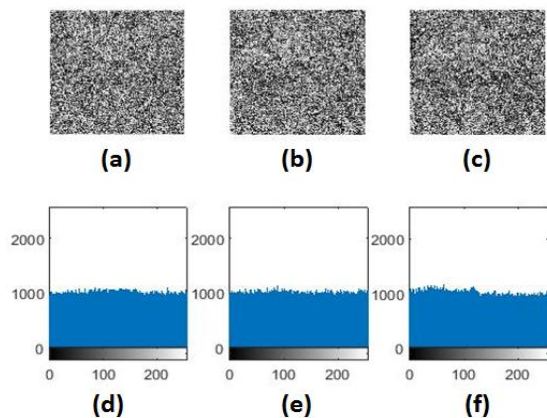
**Fig. 9** The secret image baboon, (a) Red layer, (b) Green layer, (c) Blue layer, (d) Histogram for red layer, (e) Histogram for green layer, (f) Histogram for blue layer.



**Fig.10** The secret image baboon encrypted, (a) Red layer, (b) Green layer, (c) Blue layer, (d) Histogram for red layer, (e) Histogram for green layer, (f) Histogram for blue layer..



**Fig. 11** The secret image sailboat, (a) Red layer, (b) Green layer, (c) Blue layer, (d) Histogram for red layer, (e) Histogram for green layer, (f) Histogram for blue layer.



**Fig. 12** The secret image sailboat encrypted, (a) Red layer, (b) Green layer, (c) Blue layer, (d) Histogram for red layer, (e) Histogram for green layer, (f) Histogram for blue layer.

**B. Secret Key Space**

In the proposed algorithm, three key (32 ASCII char.) are used. For each ASCII char have  $2^7$  possible values, then the proposed algorithm have  $(2^7)^{32 \times 3} = 2^{672}$  possible key size.

**C. Secret Key Sensitivity**

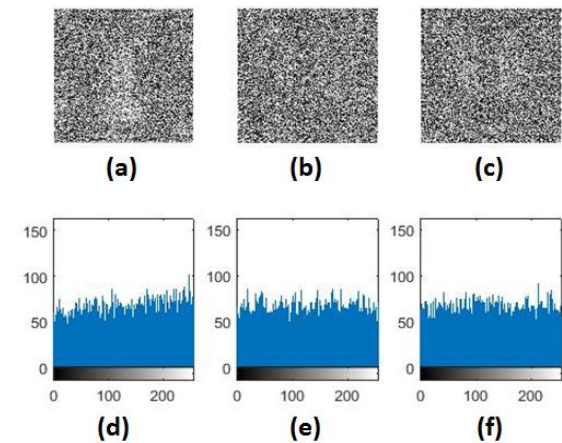
A good encryption system must be very sensitive with secret keys[15].

**Fig. 13**, show the decrypted baboon image by using the wrong key.

```
k1=Y&QBZH8ATBaCdaFEHijklZ2
3456N#9
k2=B2BB5M7#BC%+cdEfgQijNkm
1M%4567#
k3=BZHO56BZ8AAbCdeRgHiJk*1
%1234567#
```

**D. Correlation Coefficient Analysis**

Correlation values determine the relationship between original image and cipher image [15], **Table.1** show the results of the correlation between them for each layer (red, green, and blue).



**Fig. 13** The secret image baboon encrypted with wrong key, (a) Red layer, (b) Green layer, (c) Blue layer, (d) Histogram for red layer, (e) Histogram for green layer, (f) Histogram for blue layer.

**Table.1** Correlation Coefficient Of The Original And Cipher Images.

Correlation	
Layers	Correlation Result
C <sub>RR</sub>	0.000801
C <sub>RG</sub>	0.008324



Correlation	
Layers	Correlation Result
C <sub>RB</sub>	0.013390
C <sub>GR</sub>	0.004451
C <sub>GG</sub>	0.006319
C <sub>GB</sub>	0.013551
C <sub>BR</sub>	0.008920
C <sub>BG</sub>	0.006611
C <sub>BB</sub>	0.011195

### E. Information Entropy Analysis

Information entropy represents the probability of the pixel value in the original and cipher image, **Table.2** show the results of the entropy for both original and cipher image for each layer. The entropy calculated with equation below,  $p(m_i)$  denotes the probability of symbol  $m_i$  [15].

$$H(m) = \sum_{i=0}^{2^N-1} p(m_i) \log_2\left(\frac{1}{p(m_i)}\right) \quad (6)$$

**Table.2 Information Entropy Of The Original And Cipher Images.**

Information Entropy			
Image	Red	Green	Blue
Oreginal	7.248629	7.587695	6.926869
Cipher	7.996827	7.997011	7.997061

### F. Differential Analysis

NPCR (Net Pixel Change Rate) and UACI (Unified Average Changing Intensity) are two measurements to

evaluate the relationship between two encrypted images when change one pixel value of original image [15], **Table.3** show the results of the NPCR and UACI for two cipher images. The NPCR and UACI are calculated with equations below,  $c1(i)$   $c2(i)$  are the pixels of cipher image and  $N$  is the number of the pixels.

$$NPCR = \frac{\sum_{i=1}^N W(i)}{N} * 100\% \quad (7)$$

$$W(i) = \begin{cases} 0, & \text{if } c1(i) = c2(i) \\ 1, & \text{if } c1(i) \neq c2(i) \end{cases} \quad (8)$$

$$UACI = \frac{100}{N * 255} \sum_{i=1}^N |c1 - c2| \quad (9)$$

**Table.3 NPCR And UACI Results.**

NPCR and UACI			
	Red	Green	Blue
NPCR	99.560547	99.603271	99.650574
UACI	32.718482	32.767418	32.841845

In the second part, check the quality of the stego images. The PSNR is calculated from below equation [14].

$$PSNR = 10 * \log((255)^2 / MSE) \quad (10)$$

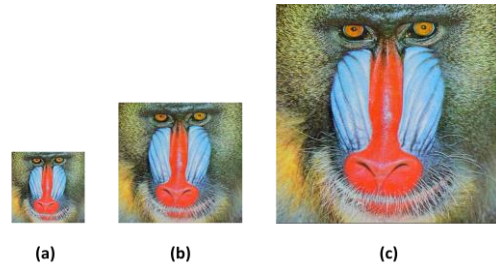
Baboon secret image with tree different size (128\*128 - 256\*256 - 512\*512) as shown in the **Fig. 14** was embedding with cover images. Four cover images from the USC-SIPI database with size 512\*512 as shown in the **Fig. 15**. The results of PSNR for the stego images are as follows in **Table. 4**, and shown in

the Fig. 16, 17, and 18. The secret image extracted from the stego images based on extraction proposed algorithm as shown in the Fig. 19.

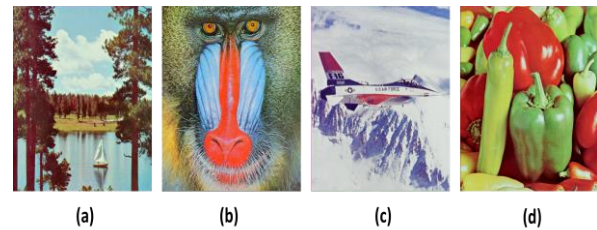
**Table.4 PSNR Result For Cover Images.**

Secret Image Size	Cover with Size 512*512	PSNR
128*128	Sailboat	62.3767 db
	Baboon	62.5201 db
	Airplane	67.9313 db
	Peppers	60.9228 db
256*256	Sailboat	54.7777 db
	Baboon	55.2847 db
	Airplane	59.5838 db
	Peppers	54.4472 db
512*512	Sailboat	44.4009 db
	Baboon	44.2718 db
	Airplane	50.0085 db
	Peppers	43.8685 db

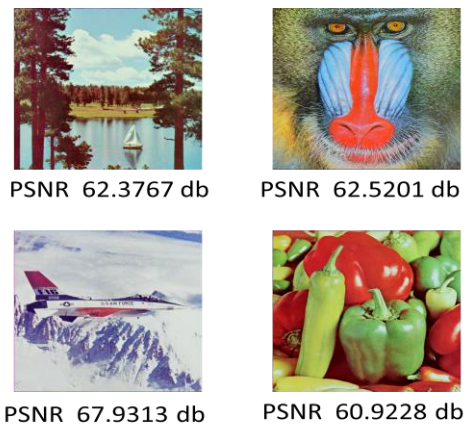
Finally, **Table. 5** summarizes the comparison between the proposed algorithm in [4] and our proposed algorithm with PSNR measure. In these algorithms, five test gray images (USC-SIPI Image Database) are used, one as secret image (Airplane Jet-F16) with size 256\*256 and four cover images (Lena, Pepper , Baboon , and Elaine) with size 512\*512.



**Fig. 14 Baboon secret image (a) Size 128\*128, (b) Size 256\*256, (c) Size 512\*512.**

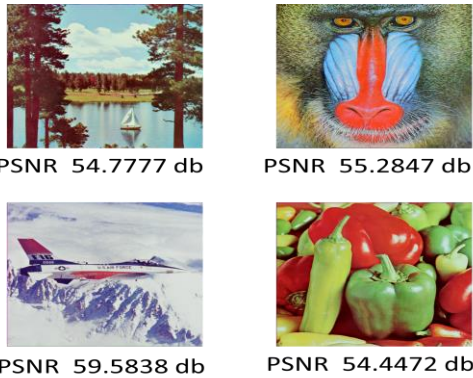


**Fig. 15 Cover images (a) Sailboat, (b) Baboon, (c) Airplane, (d) Peppers.**

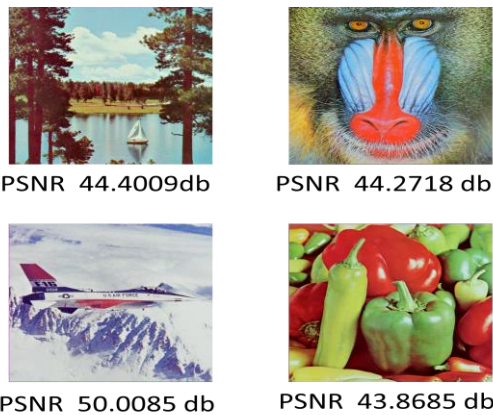


**Fig. 16 PSNR result for stego images when embedding (128\*128) secret image.**

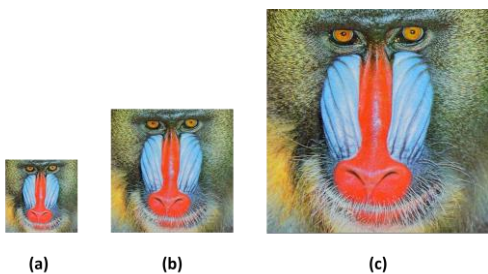
**Table.5 Comparison Between Conventional Method and Proposed Method With PSNR.**



**Fig. 17 PSNR result for stego image when embedding (256\*256) secret**



**Fig.18 PSNR result for stego image when embedding (512\*512) secret image.**



**Fig. 19. The baboon secret image after extraction (a) Size 128\*128, (b) Size 256\*256, (c) Size 512\*512.**

Methods	Cover with Size 512*512	PSNR
Conventional Method (Ref. [10])	Lena	49.47 db
	Pepper	49.47 db
	Baboon	49.50 db
	Elaine	49.51 db
Our Proposed Method	Lena	55.20 db
	Pepper	54.95 db
	Baboon	55.72 db
	Elaine	56.39 db

### 5. Conclusion

In this paper a novel method of steganography has been proposed. Which is using Lorenz chaotic map to encrypt the secret image and secret sharing scheme for secret sharing with multi-cover images. As mentioned in Sec. 3, The ISSC proposed method achieved main goals:

- 1) Achieving a high level for security, large key space for image encryption by:
  - a) Encrypts the image with sensitive encrypted key based Lorenz chaotic map in the proposed algorithm.
  - b) Sharing the secret image to four shadows based secret sharing schemes.
  - c) Embeds the secret image with Lorenz chaotic map in the proposed algorithm.



2) high payload capacity reached to 0.75 M of pixels that embedding in four cover images size (512\*512) with quality reached to 44 db of PSNR.

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## نهجا يرتكز على أخفاء صورة سرية ملونة مبنية على مخطط مشاركة متعددة التغطية

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### الخلاصة:

التشفير والتخزين هي التقنيات الرئيسية المستخدمة لتأمين المعلومات أثناء الاتصالات. تقترح هذه الورقة خوارزمية للتشفير والتدريج على أساس تقاسم الصور ونظام الفوضى، حيث تم تطبيق هذه الخوارزمية لأداء ثلاث عمليات. أولاً، تشفير الصورة السرية الملونة على أساس مبدأ لورينز (خريطة الفوضى). ثم، تقاسم الصورة المشفرة إلى عدد غير محدد من بيانات الظل على أساس مخطط تقاسم السرية. أخيراً، تضمين هذا العدد من بيانات الظل مع عدد من صور الغطاء. تم استخدام العديد من التحليل الأمني لتشفير الصور، مثل سعة وحساسية المفتاح السري، الرسم البياني، مدى الترابط بين البيانات المشفرة، الإنتروبيا، والتحليل التفاضلي. وتستخدم نسبة ذروة الإشارة إلى الضوضاء لاختبار وقياس نوعية وأداء صور الغلاف للخوارزمية المقترحة. تم تطبيق الخوارزمية المقترحة في هذا البحث فكانت الخوارزمية المقترحة لديها مستوى عال للأمن، سعة وحساسية المفتاح السري، سعة حجم البيانات السرية تصل الى 0.75 MB المضمنه داخل اربع من صور الغطاء ذات حجم 512\*512, مع الحفاظ على جودة صور الغطاء التي تصل الى 44 db من نسبة ذروة الاشارة الى الضوضاء.